





Kill both Spatial and Temporal shifts





🚳 🎑 with one STONE 🚳 🕮





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Spatio-temporal OOD prediction problem





♦ Objective

Default prediction:

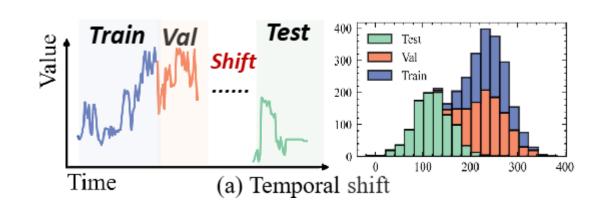
$$\min_{\mathcal{F}} \mathbb{E}_{(\mathbf{x},\mathbf{y}) \sim P(\mathbf{x},\mathbf{y}|e)} [\mathcal{L}(\mathcal{F}(\mathbf{x},\mathcal{G}),\mathbf{y})]$$

❖ OOD prediction:

$$\min_{\mathcal{F}} \max_{e^* \in E} \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim P(\mathbf{x}, \mathbf{y} | e^*)} [\mathcal{L}(\mathcal{F}(\mathbf{x}, \mathcal{G}), \mathbf{y})]$$

♦ Challenges

- ❖ Temporal shift.
- Spatial shift.



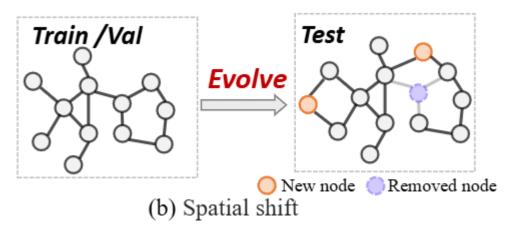


Figure 1. Visualization of temporal (a) and spatial (b) shifts.

Spatio-temporal environments shifts





♦ Portray and perceive

Semantic graph: A suitable metric is utilized to portray the temporal or spatial similarity between nodes at the current time.

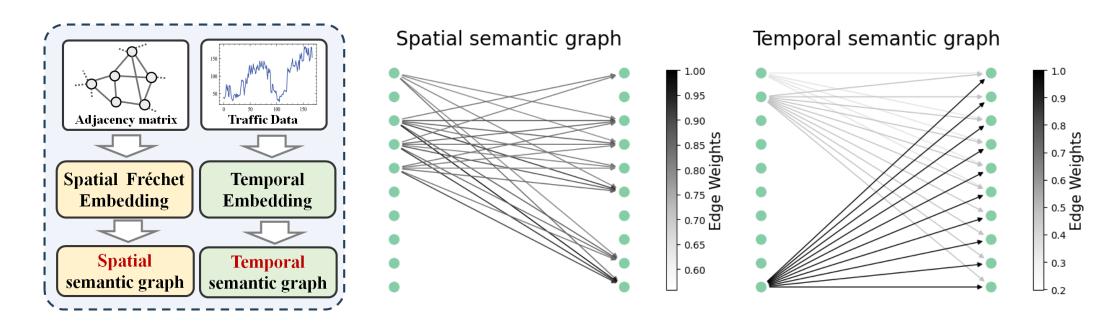


Figure 2. Spatial and Temporal semantic graphs.

Spatio-temporal environments shifts





♦ The case of traffic prediction

- ❖ Node #0 ~ #4 in SD.
- Similarity of DTW distances based on 12 time steps.

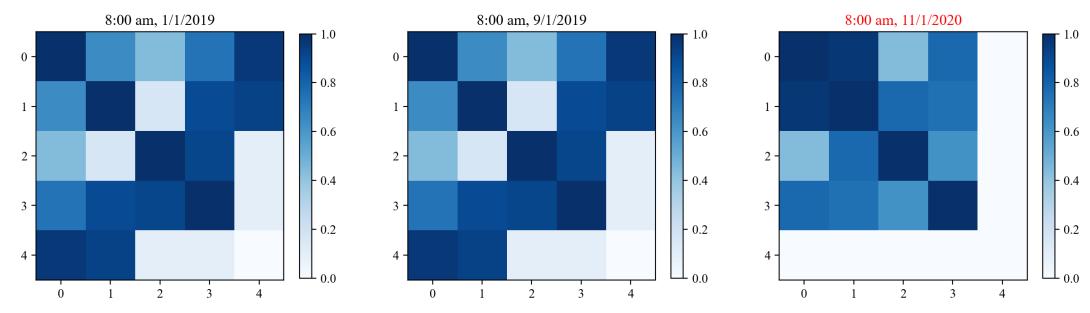


Figure 3. Case study of #1 to #5 sensors in SD datasets.

Spatial Side Information





♦ Bourgain's Theorem (1985)

 \clubsuit If (X, d) is an N-point metric space and f is an Fréchet embedding, then

$$\frac{1}{\mathcal{O}(\log N)}d(x,y) \le \mathbb{E}_f \|f(x) - f(y)\| \le d(x,y), \forall x,y \in X.$$

♦ Spatial Fréchet Embedding

- Dimension is not affected by the addition of new nodes.
- ❖ Solid Theory.
- ❖ Based on Hamming distance. Low complexity.

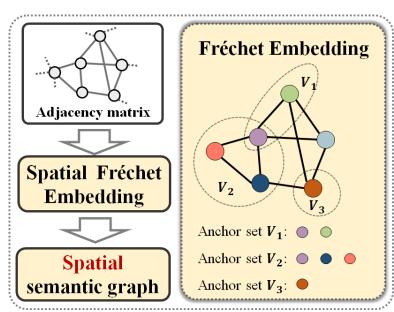


Figure 4. Fréchet Embedding

Environment Generators





♦ Optimized objects for multiple environments

* Mask operators M for disturbing spatio-temporal environment in training phase.

$$\min_{\Theta} \operatorname{Var}\{\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x},\mathcal{G}),\mathbf{y}|\mathbb{M}^{*},\Theta)\} + \beta \mathbb{E}[\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x},\mathcal{G}),\mathbf{y}|\mathbb{M}^{*},\Theta)]),$$
s.t. $\mathbb{M}^{*} = (\mathbb{M}_{1}^{*},\mathbb{M}_{2}^{*},...,\mathbb{M}_{K_{M}}^{*}) = \underset{\mathbb{M}_{m} \in \{0,1\}^{N \times N}}{\operatorname{argmax}} \operatorname{Var}\{\mathcal{L}_{\Theta}(\mathcal{F}(\mathbf{x},\mathcal{G}),\mathbf{y}|\mathbb{M}^{m},\Theta)\}.$

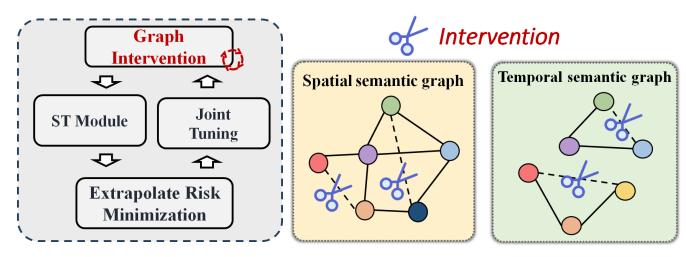


Figure 5. Mask operators and optimization.





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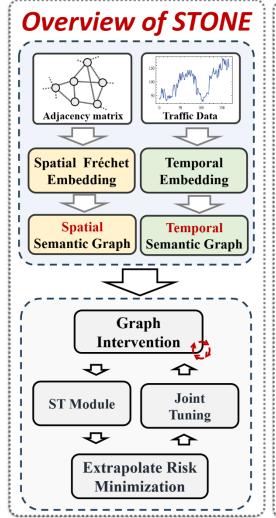


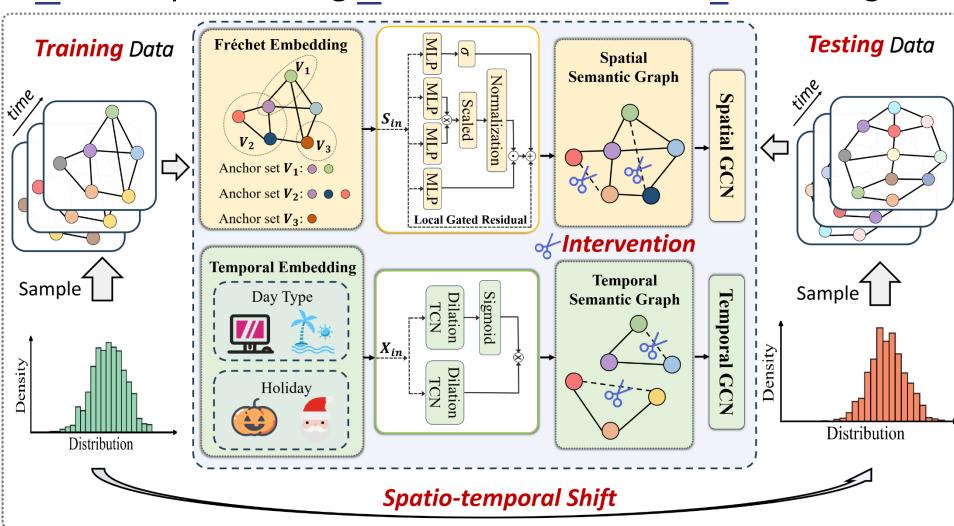






Spatio-Temporal OOD Graph Learning Networks with Fréchet Embedding





Experiments for STONE





♦ Datasets: SD and GBA in LargeST under OOD setting

- [1/1/2019, 8/31/2019] for training,
 [9/1/2019, 10/31/2019] for validation,
 [11/1/2020, 12/31/2020] for test, etc.
- ❖ Vertices increases by **5**%/**10**%/**15**% and decreases by **5**% in validation and test sets.
- **STONE** exhibits a relative improvement of up to nearly **20%**.
- * Result details in paper.















